Final Review: #19 on the final review sheet: Let f(x) = \(\times t \sin(t^3) dt. Compute f''(0). -> find Maclanrin Series for f(x): · t. Sin (t3) = t. \(\frac{\(-1\)^{n} (t^{3})^{2n+1}}{N=0} \) • $f(x) = \frac{2}{\sqrt{(2N+1)!}} \frac{(-1)^{N} t^{6N+4}}{\sqrt{(2N+1)!}}$ • $f(x) = \frac{(-1)^{N}}{\sqrt{(2N+1)!}} \frac{(-1)^{N}}{\sqrt{(2N+1)!}} \frac{t^{6N+5}}{\sqrt{(2N+5)!}}$ = $\frac{2}{\sqrt{(-1)^{N}}} \frac{(-1)^{N}}{\sqrt{(2N+1)!}} \frac{t^{6N+5}}{\sqrt{(2N+5)!}}$ $=\frac{2}{2}\frac{(-1)^{N}}{(-1)^{N}$ -> By Taylor's theorem: $f(x) = \sum_{n=1}^{\infty} f^{(n)}(0) \times x^{n} \quad (**)$ Tegnale the coefficients of X" in (*) and (**):

$$\frac{(4)}{(-1)} \cdot \frac{1}{3!} = \frac{f^{(1)}(0)}{11!} = \frac{11!}{11!} = \frac{11!}{11!} = \frac{10!}{11!} = \frac{10!}{3!}$$

#2(c) on the midtern review:

$$T = \int \left(\frac{e^{5z} + x^{5z}}{5x}\right) dx$$

$$= e^{5z} \left(\frac{x^{-1/2}}{x^{2}}\right) dx + \int x^{5z-1/2} dx$$

$$= e^{5z} \frac{x^{1/2}}{x^{2}} + \frac{x^{5z+1/2}}{5z+1/2} + C$$

#2(d) on the midterm review:

$$T = \int \left(\frac{2}{3x} - \frac{1}{\sqrt{4-x^2}}\right) dx$$

$$= I_1 - I_2$$

$$I_1 = \frac{2}{3} \int \frac{dx}{x} = \frac{2}{3} \ln |x| + C_1$$

$$I_{2} = \int \frac{dx}{Jy-x^{2}} = \int \frac{dx}{ZJI-(\frac{x}{k})^{q}} \frac{n-snb}{n=\frac{x}{2}}$$

$$= \int \frac{dn}{JI-n^{2}} = Sin'(n) + C_{2}$$

$$= Sin'(\frac{x}{2}) + C_{2}$$

$$I = I_{1} - I_{2} = \frac{2}{3}ln/xI - Sin'(\frac{x}{2}) + C$$

$$I = \int \frac{4}{(x-1)^{2}} dx, \text{ evaluate } I \text{ using}$$

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Then
$$I = \lim_{N \to \infty} S_N = 2(1+2+\frac{8}{6})$$

$$= \frac{26}{3}$$

$$\Rightarrow \text{ check our work:}$$

$$I = \int_{2}^{4} (x-1)^2 dx = \frac{(x-1)}{3} \Big|_{2}^{4}$$

$$= \frac{3^3}{3} - \frac{1}{3} = \frac{26}{3}$$

$$\# 12 \text{ on the midlerm review sheet:}$$

$$F(x) = \int_{\frac{8}{x}}^{x} \frac{t}{1-5t} dt$$

$$f \text{ ind } F(2).$$

$$G(x) = \int_{a}^{x} \frac{t}{1-5t} dt$$

By the FTC, $G'(x) = \frac{x}{1-\sqrt{x}}$ By the other FTC,

$$F(x) = G(x^{2}) - G(\frac{8}{x})$$

$$F'(x) = \frac{1}{4x} \left[F(x) \right] = G'(x^{2})(2x)$$

$$-G'(\frac{8}{x})(-\frac{8}{x^{2}})$$

$$= (2x) \frac{x^{2}}{1-x} + \frac{8}{x^{2}} \cdot \frac{8}{x} \cdot \frac{1}{1-\sqrt{8x}} (*)$$

$$So by (*)$$

$$F'(z) = \frac{4 \cdot 4}{-1} + \frac{64}{8} \cdot \frac{1}{1-\sqrt{4}}$$

$$= -16 + 8(-1) = -24$$

$$\frac{1}{4} |S(a)| \text{ on the midlern review:}$$

$$I = \left(\frac{1}{x^{2}} |Sec(\frac{1}{x})| + an(\frac{1}{x}) dx \right)$$

$$T = \int \frac{1}{x^2} \operatorname{Sec}(\frac{1}{x}) \tan(\frac{1}{x}) dx$$

$$n-\operatorname{Snb}: n = \frac{1}{x}, dn = -\frac{dx}{x^2}$$

$$\iff \frac{dx}{x^2} = -dn$$

$$= -\int \operatorname{Sec}(n) + C$$

 $= - Sec(\frac{1}{x}) + C$

16(b) on the midter in review: $n-sub: n = 4-3e^{2x}$ $dn = -6e^{2x} dx \iff e^{2x} dx = -\frac{1}{6} dn$ $=-\frac{1}{6}\left(\frac{dn}{\sqrt{n}}=-\frac{1}{6}\frac{\sqrt{n}}{\frac{1}{2}}+C\right)$ $= -\frac{1}{3} \int \pi + C = -\frac{1}{3} \int 4^{-3}e^{2x} + C$ #22(d) on the midlern review: $n-snb: n=x^2, dn=2xdx$ $I=\int x^3 e^{x^2} dx$ $x^3 dx = \frac{1}{z} n du$ IBP: · (ndv=nv- (vdn $=\frac{1}{2}$ \ neⁿ dn · how to choose n! = 1 [ne" - Se" dn ch=endu $=\frac{1}{Z}ne^{n}-\frac{1}{Z}e^{n}+C$ $y = e^{u}$ an= an

 $=\frac{1}{2}\left(x^{2}e^{x^{2}}-e^{x^{2}}\right)+\left(\frac{1}{2}\left(x^{2}+e^{x^{2}}-e^{x^{2}}\right)+\left(\frac{1}{2}\left(x^{2}+e^{x^{2}}-e^{x^{2}}\right)+\left(\frac{1}{2}\left(x^{2}+e^{x^{2}}-e^{x^{2}}\right)+\left(\frac{1}{2}\left(x^{2}+e^{x^{2}}-e$

#23(b) on the midterm review: $I = \begin{cases} S_{iN}^{5}(2x) \cos^{3}(2x) dx \\ S_{iN}^{5}(2x) \cos^{3}(2x) dx \end{cases}$ $= \begin{cases} cos^{3}(2x) = cos(2x) (1 - S_{NN}^{2}(2x)) \\ 1 - S_{NN}^{5}(2x) \end{cases} dn = 2 cos(2x) dx$ $= \begin{cases} 1 \\ 1 \end{cases} \begin{cases} 1 - n^{2} \\ 1 \end{cases} dn = \frac{1}{2} \left(\frac{n^{6}}{6} - \frac{n^{8}}{8} \right) + C$ $= \begin{cases} S_{iN}^{6}(2x) \\ 12 \end{cases} - \frac{S_{iN}^{8}(2x)}{16} + C$